

Lesson 8: Factor Difference of Squares

A special type of polynomial that has two squares joined by a subtraction sign also known as a “difference of squares” can be factored with two conjugate binomials.

To find the factors take the square root of each of the terms. One binomial you **add** the roots, the other you **subtract**.

$$m^2 - n^2 = (m+n)(m-n)$$

Examples: Factor.

$$1) \quad x^2 - 9 = (x)^2 - (3)^2 = (x-3)(x+3)$$

$$2) \quad x^2 - 36 = (x+6)(x-6)$$

$$3) \quad 64a^2 - 49 = (8a+7)(8a-7)$$

$$4) \quad 16x^2 - 25y^2 = (4x+5y)(4x-5y)$$

$$5) \quad x^4 - 81 = (x^2 + 9)(x^2 - 9)$$

↙ factor further!

$$= (x^2 + 9)(x+3)(x-3)$$

Always look for a GCF!

$$6) \frac{8x^2}{8} - \frac{32}{8} = 8(x^2 - 4) = 8(x+2)(x-2)$$

$$\text{GCF} = 8$$

$$7) \frac{xy^2}{x} - \frac{x^3}{x} = x(y^2 - x^2) = x(y+x)(y-x)$$

$$\text{GCF} = x$$

$$8) \frac{3a^3}{3a} - \frac{12ab^2}{3a} = 3a(a^2 - 4b^2) = 3a(a+2b)(a-2b)$$

$$\text{GCF} = 3a$$

$$9) x^4 - 12x^2 - 64 = (x^2 + 4)(x^2 - 16)$$

$$= (x^2 + 4)(x + 4)(x - 4)$$

factored further!

$$\begin{array}{r} 4 \times \begin{array}{l} -12 \\ -16 \\ -64 \end{array} \end{array}$$

$$1 \quad 64$$

$$2 \quad 32$$

$$8 \quad 8$$

Worksheet